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Let $a < c < b$, $a, b, c \in R$.

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

$\because f'(c) \neq 0, \Rightarrow f(b) - f(a) \neq 0$

$\therefore f(a) \neq f(b)$